# Econ 133 - Global Inequality and Growth <br> Optimal labor income taxation 

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## What we're going to learn in this lecture:

- How labor income taxes have changed over time
- The equity-efficiency trade-off that government face when taxing labor income
- The determinants of optimal labor income tax rates

Top income tax rates, 1900-2013


## 1 The equity-efficiency trade-off

When the government taxes labor income, this has two effects

- Generates tax revenue: mechanical (positive) revenue effect
- Workers respond by reducing labor supply: behavioral (negative) revenue effect


## The optimal labor income tax problem

Goal of gov. is to balance the equity gains with the efficiency losses

- Objective: A social welfare function (SWF), $W=W\left(U_{1}, \ldots, U_{n}\right)$, where $U_{i}$ is the utility of individual $i$.
- Instrument: A tax function $T(z)$ that gives the amount of taxes owed by individual with earnings $z$
- Contraints: gov. budget constraint and indiv.optimizing behavior
- The problem: Design $T($.$) to maximize SWF subject to the$ government budget constraint and individual optimization
- This problem was first solved by Mirrlees (1971). In its general form, it is difficult to solve.
- We will simplify the problem by:

1. Simplifying the tax system: piecewise linear taxes
2. Considering a special social welfare function

## Simplification number one: linear income tax

- The simplest tax system is one with a constant marginal tax rate $\tau$ and a guaranteed minimum income $G>0$ :

$$
\begin{equation*}
T(z)=\tau \cdot z-G . \tag{1}
\end{equation*}
$$

- Also known as a flat tax
- The average tax rate is given by $\frac{T(z)}{z}=\tau-\frac{G}{z}$.


## Simplification number two: Rawlsian SWF

- The Rawlsian SWF is $W=\min \left(U_{1}, \ldots, U_{n}\right)$ : gov. only cares about the worst-off individual in the population
- Let's assume that the worst-off individual in the population is not able to work hence live off the transfer $G$
- A Rawlsian government then wants to maximize $G \Rightarrow$ the optimal income $\operatorname{tax} \tau$ maximizes revenue $\Rightarrow$ rech top of the Laffer curve.


## THE LAFFER CURVE

Tax revenue $R$


Laffer curve is important in two ways:

- Laffer rate is the optimum under Rawlsian social preferences
- Laffer rate represents upper bound on optimal tax rates:
- If the goal is to maximize tax revenue
- But other goals are possible


## 2 The optimal income tax rate

## Laffer rate under linear taxation

- Theorem: the Laffer rate is given by $\tau^{*}=\frac{1}{1+\varepsilon}$
- where $\varepsilon \equiv \frac{d z / z}{d(1-\tau) /(1-\tau)}$ is the the elasticity of taxable income
- With $\varepsilon \approx 0.2$ then $\tau^{*} \approx 83 \%$

If taxable income is completely inelastic, then the optimal linear tax rate on labor income is:

A-100\%

B-83\%

C - $100 \%$ if the social welfare function is Rawlsian

D - Indeterminate

## Piecewise linear tax systems

- Most tax systems are not linear, but piecewise linear: impose different marginal tax rates over different income intervals
- Within each bracket, the marginal tax rate is constant. Across brackets, marginal tax rates differ and typically increase with $Y_{L}$
- Let's focus on the Laffer rate in the highest-income tax bracket, assuming that income is Pareto-distributed at the top
- Variables pertaining to top-rate taxpayers are denoted by "hat"
- Theorem: the high-income Laffer rate is given by

$$
\hat{\tau}^{*}=\frac{1}{1+\hat{\varepsilon} \cdot a}
$$

- where $\hat{\varepsilon}$ is the elasticity of taxable income at the top
- And $a=$ Pareto coefficient
- The more unequal the distribution of income, the higher the optimal top marginal income tax rate
- The higher the elasticity of taxable income, the lower the optimal top marginal income tax rate
- Plugging real number in the formula:
- If $a \approx 2$ and $\hat{\epsilon} \approx 0.2$ then $\hat{\tau}^{*} \approx 71 \%$


## 3 Summary

- There has been dramatic changes in top labor income tax rates over time
- When determining tax policy, there is a trade-off between equity and efficiency
- Two key principles of optimal taxation:

1. Don't taxe what is elastic
2. The more inequality, the higher the optimal tax rate at the top

## References

Piketty, Thomas and Emmanuel Saez "Optimal labor income taxation", Handbook of Public Economics, 2013 (web)

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