

Capital is Back: Wealth-Income Ratios in Rich Countries 1700-2010

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How do wealth-income and capital-output ratios evolve in the long-run and why?

- ▶ Impossible to address this question until recently: national accounts mostly about flows, not stocks
- ▶ We have compiled a new database of national balance sheets to address it

Table 1: A new macro database on income and wealth

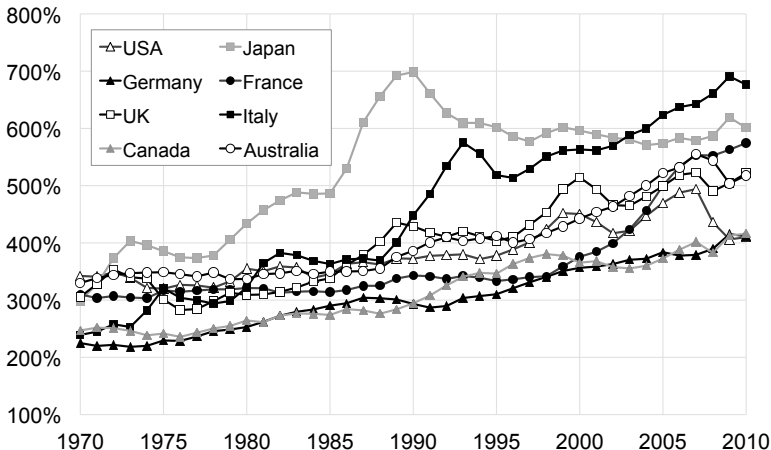
	Total period covered in database	Annual series	Decennial estimates
U.S.	1770-2010	1869-2010	1770-2010
Japan	1960-2010	1960-2010	
Germany	1870-2010	1870-2010	
France	1700-2010	1896-2010	1700-2010
U.K.	1700-2010	1855-2010	1700-2010
Italy	1965-2010	1965-2010	
Canada	1970-2010	1970-2010	
Australia	1970-2010	1970-2010	

The wealth and income concepts we use

- ▶ Private wealth W = assets - liabilities of households (corporations valued at market prices through equities)
- ▶ Government wealth W_g
- ▶ Market-value national wealth $W_n = W + W_g$
- ▶ $W_n = K$ (land+housing+other domestic K) + NFA
- ▶ Domestic output $Y_d = F(K, L)$ (net of depreciation)
- ▶ National income $Y = Y_d + rNFA$
- ▶ Private wealth-national income ratio $\beta = W/Y$
- ▶ National wealth-national income ratio $\beta_n = W_n/Y$
- ▶ Capital-output ratio $\beta_k = K/Y_d$

We find a gradual rise of private wealth-national income ratios since 1970

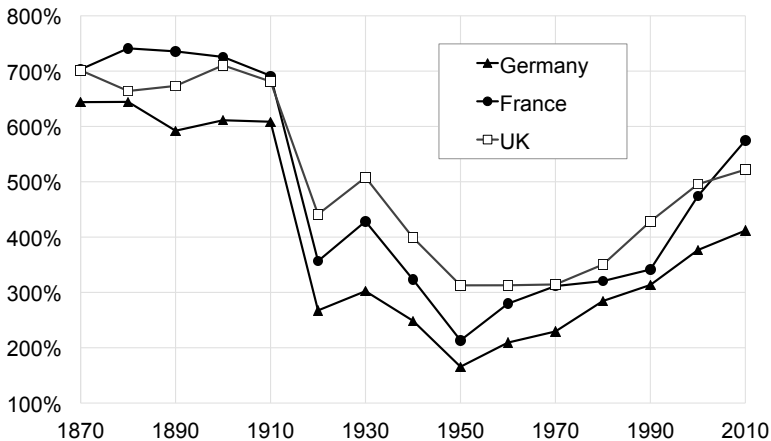
Figure 1: Private wealth / national income ratios 1970-2010



Authors' computations using country national accounts. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors)

European ratios appear to be returning to their high 18c-19c values...

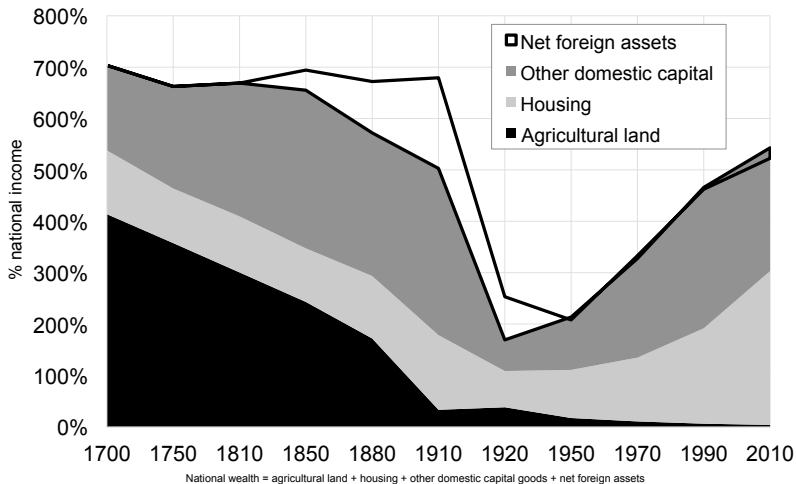
**Figure 2: Private wealth / national income ratios in Europe
1870-2010**



Authors' computations using country national accounts. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors). Data are decennial averages (1910-1913 averages for 1910)

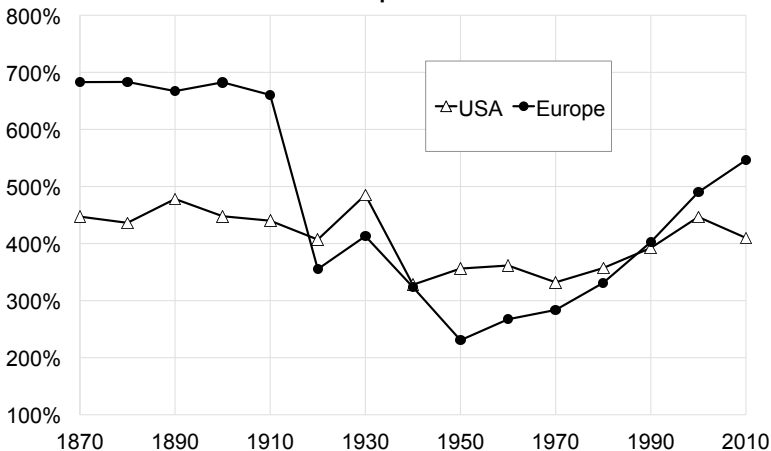
Despite huge changes in the nature of wealth

**Figure 3: The changing nature of national wealth: UK
1700-2010**



US evolution is also U-shaped but less so

**Figure 4: Private wealth / national income ratios 1870-2010:
Europe vs. USA**



Authors' computations using country national accounts. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors). Data are decennial averages (1910-1913 averages for Europe)

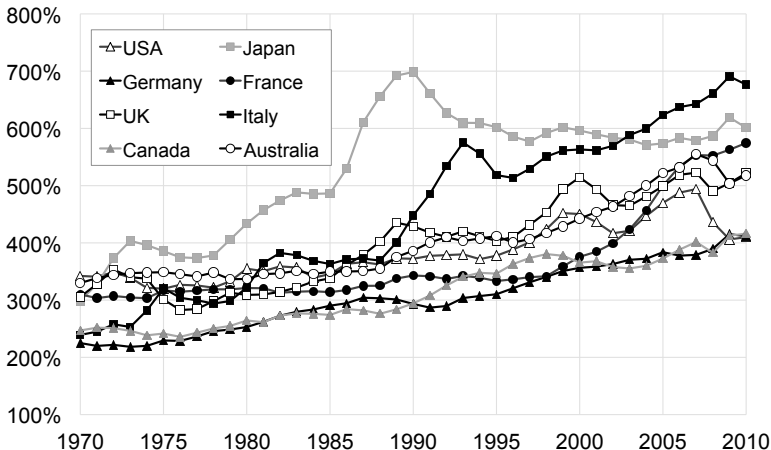
Outline of the talk

1. The 1970-2010 rise of wealth-income ratios
2. The 1870-2010 U-shaped evolution of wealth-income ratios
3. The changing nature of wealth 1700-2010
4. Implications of the return of high wealth-income ratios

I- The 1970-2010 rise of
wealth-income ratios

1970-2010: general rise of private wealth, with interesting cross-country variations

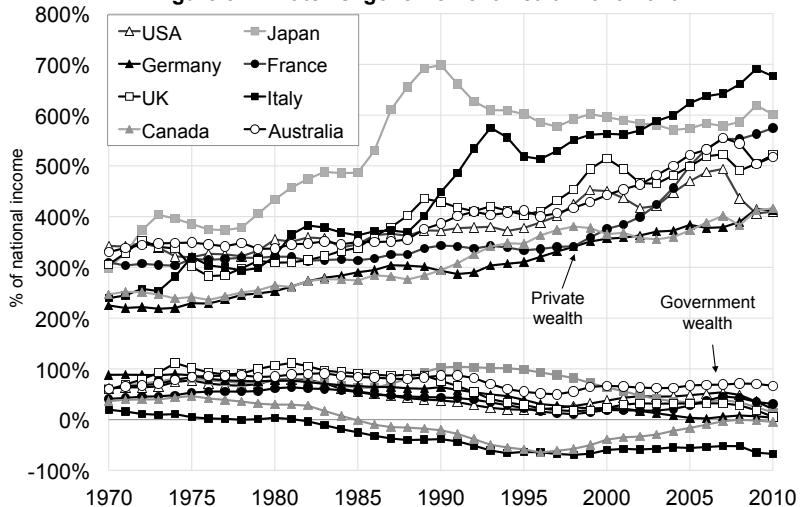
Figure 1: Private wealth / national income ratios 1970-2010



Authors' computations using country national accounts. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors)

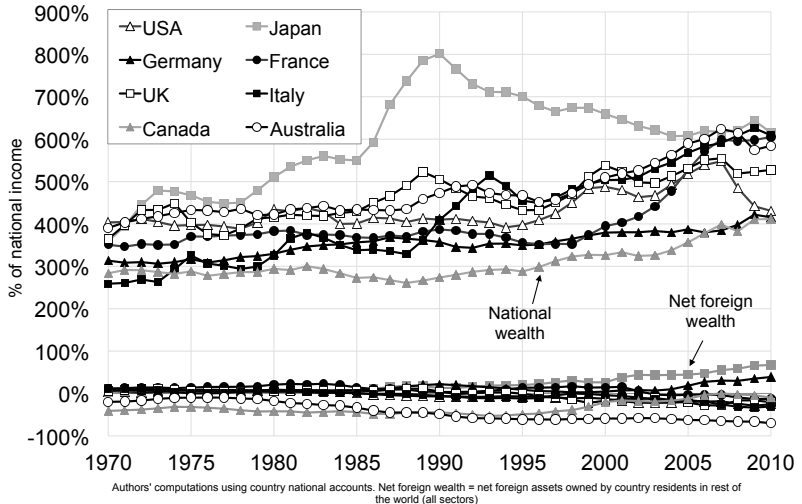
Rise of private wealth has been larger than decline of government wealth...

Figure 5: Private vs. government wealth 1970-2010



...So that national wealth has also increased

Figure 6: National vs. foreign wealth, 1970-2010



How can we explain 1970-2010 rise of β ?

Two key factors:

1. **Slowdown of productivity and pop. growth**, in line with Harrod-Domar-Solow formula $\beta = s/g$:
 - ▶ In the long-run, wealth-income ratio $\beta = s/g$
 - ▶ If $s = 10\%$ and $g = 3\%$ then $\beta \approx 300\%$
 - ▶ But if $s = 10\%$ and $g = 1.5\%$ then $\beta \approx 600\%$
 - ▶ $g = \text{productivity} + \text{pop. growth}$
2. **A rise in relative asset prices**, itself driven by changes in capital policies since world wars

Factor 1: Growth slowdown

A quick refresher on the Harrod-Domar-Solow formula:

- ▶ $W_{t+1} = W_t + s_t Y_t$
- ▶ $\beta_{t+1} = \beta_t(1 + g_{wst})/(1 + g_t)$
 - ▶ $1 + g_{wst} = 1 + s_t/\beta_t$ = saving-induced wealth growth rate
 - ▶ $1 + g_t = Y_{t+1}/Y_t$ = output growth rate (productivity + pop)
- ▶ In steady state, with fixed saving rate $s_t = s$ and growth rate $g_t = g$:
 $\beta_t \rightarrow \beta = s/g$ (**Harrod-Domar-Solow formula**)
- ▶ True in the steady-state of any one-good model of capital accumulation
- ▶ True wherever s comes from

$\beta \rightarrow s/g$ is true wherever s comes from

Production: $Y_{dt} = F(K_t, L_t)$ with $L_t = L_0 e^{gt}$. Utility:

► **If wealth or bequest in the utility function**

$V(c, b) = c^{1-s} b^s$ then saving rate is set by taste for wealth s (and demography if life-cycle saving)

► **If dynastic utility** $V = \int e^{-\theta t} c_t^{1-\gamma} / (1-\gamma)$ then
 $r = \theta + \gamma g$ and $\beta = \alpha / r = \alpha / (\theta + \gamma g) \nearrow$ as $g \searrow$



In all cases, $\beta = s/g$ increases as $g \searrow$

Factor 1: Growth slowdown (continued)

$\beta = s/g$ helps understand some key features of the data:

- ▶ Large fraction of rise in β in low-growth countries (Japan, Europe)
- ▶ Europe vs. US difference

With low growth, β may become very high in the whole world

- ▶ But no reason why β should reach any specific value
- ▶ All values possible in steady-state because s and g vary for all sorts of reasons

Because s and g vary for many independent reasons, β can vary a lot across countries

Table 2: Growth rate vs private saving rate in rich countries, 1970-2010

	Real growth rate of national income	Population growth rate	Real growth rate of per capita national income	Net private saving rate (personal + corporate) (% national income)
U.S.	2.8%	1.0%	1.8%	7.7%
Japan	2.5%	0.5%	2.0%	14.6%
Germany	2.0%	0.2%	1.8%	12.2%
France	2.2%	0.6%	1.6%	11.1%
U.K.	2.2%	0.3%	1.9%	7.3%
Italy	1.9%	0.3%	1.6%	15.0%
Canada	2.8%	1.1%	1.7%	12.1%
Australia	3.2%	1.4%	1.7%	9.9%

Authors' computations using country national accounts. Growth rates are geometric averages and for income use chain-weighted GDP deflators. For alternative deflators, see Appendix Table A3 and Country Tables US.3, JP.3, etc. 1970-2010 average saving rates are obtained by weighting yearly saving rates by real national income.

Factor 2: The role of asset prices

Consider now a two-goods model (one capital and one consumption good):

- ▶ Define $1 + q_t$ = real rate of capital gain (or loss) = excess of asset price inflation over consumer price inflation
- ▶ Then $\beta_{t+1} = \beta_t(1 + g_{wst})(1 + q_t)/(1 + g_t)$
 - ▶ $1 + g_{wst} = 1 + s_t/\beta_t$ = saving-induced wealth growth rate
 - ▶ $1 + q_t$ = capital-gains induced wealth growth rate

Is the rise of β mostly due to saving or capital gains?

Our strategy to identify the source of the rise of β :

- ▶ We decompose the evolution of β into 2 multiplicative components:

$$\beta_{t+1} = \frac{(1 + g_{wst})(1 + q_t)}{1 + g_t} \beta_t$$

- ▶ We do not specify where q_t comes from and infer it from the data at our disposal on $\beta_t \dots \beta_{t+n}$, $s_t \dots s_{t+n}$ and $g_t \dots g_{t+n}$

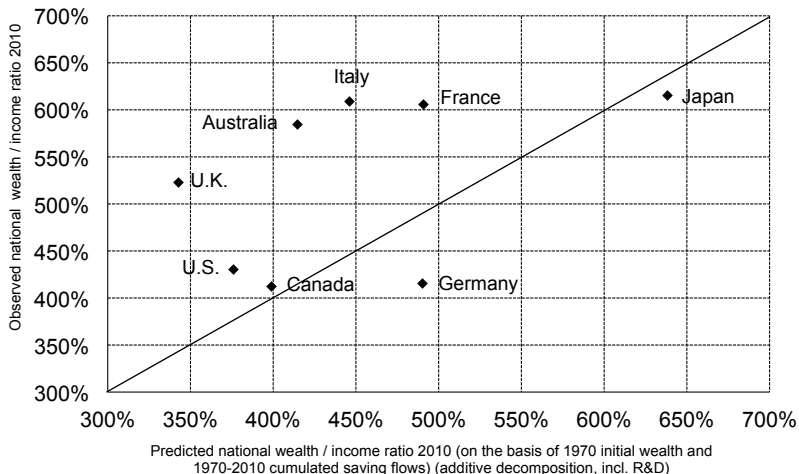
We find a clear pattern of positive K gains

Table 4: Accumulation of national wealth in rich countries, 1970-2010

	National wealth-national income ratios		Decomposition of 1970-2010 wealth growth rate		
	β (1970)	β (2010)	Real growth rate of national wealth	Savings-induced wealth growth rate	Capital-gains-induced wealth growth rate
			g_w	$g_{ws} = s/\beta$	q
U.S.	404%	431%	3.0%	2.1% 72%	0.8% 28%
Japan	359%	616%	3.9%	3.1% 78%	0.8% 22%
Germany	313%	416%	2.7%	3.1% 114%	-0.4% -14%
France	351%	605%	3.6%	2.7% 75%	0.9% 25%
U.K.	314%	523%	3.5%	1.5% 42%	2.0% 58%
Italy	259%	609%	4.1%	2.6% 63%	1.5% 37%
Canada	284%	412%	3.8%	3.4% 89%	0.4% 11%
Australia	391%	584%	4.2%	2.5% 61%	1.6% 39%

Rising asset prices played an important role in Europe, except in Germany

Figure 7a: Observed vs. predicted national wealth / national income ratios (2010)



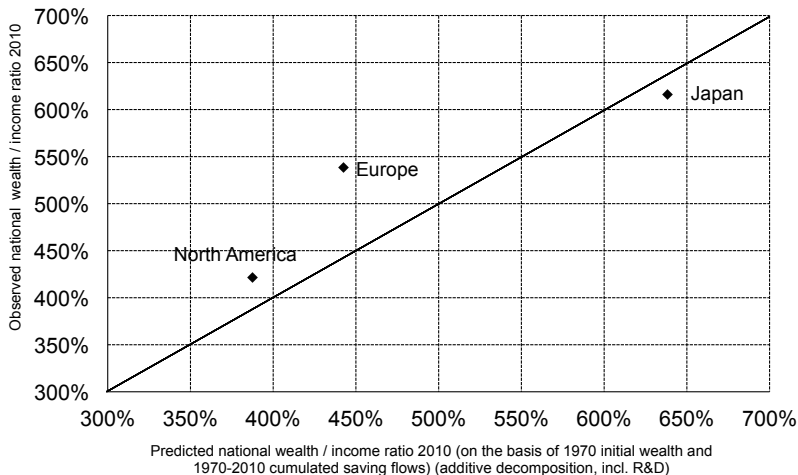
The two sources of capital gains: domestic (Europe) vs. foreign (U.S.)

Table 6: National wealth accumulation in rich countries: domestic vs. foreign capital gains

	1970-2010 capital gains on national wealth (% of 2010 national income)	Decomposition of 1970-2010 capital gains	
		Domestic wealth	Foreign wealth
U.S.	105%	72%	33%
Japan	27%	45%	-18%
Germany	-25%	-3%	-22%
France	164%	179%	-15%
U.K.	235%	217%	18%
Italy	213%	240%	-27%
Canada	63%	55%	7%
Australia	220%	178%	41%

At a very aggregated level, key force is s/g

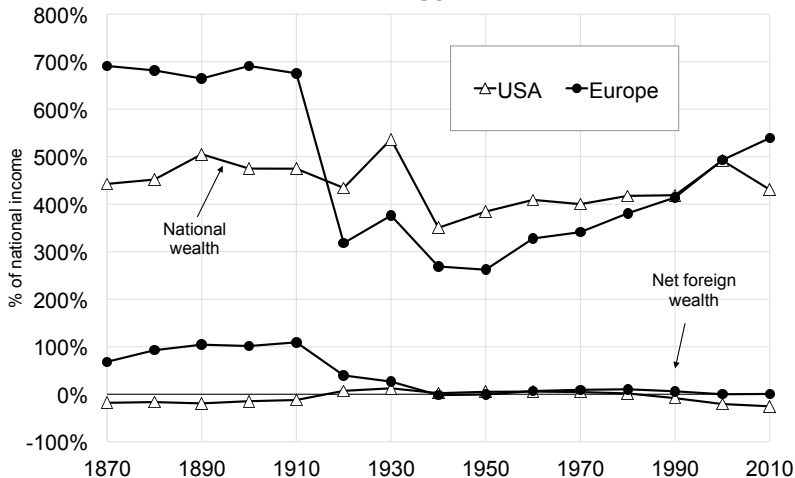
Figure 7b: Observed vs. predicted national wealth / national income ratios (2010)



II- The 1870-2010 U-shaped evolution of wealth-income ratios

How can we explain 1870-2010 evolution?

Figure 8: National and foreign wealth 1870-2010: Europe vs. USA



Asset prices decreased a lot in the interwar, and then recovered

Table 9: Accumulation of national wealth: US, UK, Germany, France, 1870-2010

	Market-value national wealth-national income ratios		Real growth rate of national wealth	Savings-induced wealth growth rate (incl. war destructions)	Capital-gains-induced wealth growth rate
	β_t	β_{t+n}	g_w	$g_{ws} = s/\beta$	q
	Panel D: France				
1870-2010	689%	605%	2.0%	1.8% 91%	0.2% 9%
1870-1910	689%	747%	1.3%	1.4% 103%	0.0% -3%
1910-2010	747%	605%	2.2%	2.0% 89%	0.3% 11%
1910-1950	747%	261%	-1.2%	-0.1% 8%	-1.1% 92%
1950-1980	261%	383%	5.9%	4.7% 80%	1.2% 20%
1980-2010	383%	605%	3.4%	2.2% 65%	1.2% 35%

In the very long run, seems like no big relative price divergence

Table 8: Accumulation of national wealth in rich countries, 1870-2010

	Market-value national wealth-national income ratios		Real growth rate of national income g	Decomposition of 1870-2010 wealth growth rate		
	β (1870)	β (2010)		Real growth rate of wealth g_w	Savings-induced wealth growth rate $g_{ws} = s/\beta$	Capital-gains-induced wealth growth rate q
U.S.	413%	431%	3.4%	3.4%	2.6% 76%	0.8% 24%
Germany	745%	416%	2.3%	2.0%	2.6% 128%	-0.6% -28%
France	689%	605%	2.1%	2.0%	1.8% 91%	0.2% 9%
U.K.	656%	523%	1.9%	1.8%	1.6% 89%	0.2% 11%

The real growth rate of national wealth has been 3.4% per year in the U.S. between 1870 and 2010. This can be decomposed into a 2.6% savings-induced growth rate and a 0.8% residual term (capital gains and/or measurement errors).

Authors' computations using country national accounts. War destructions & other volume changes were included in savings-induced wealth growth rate. For full decomposition, see Appendix Country Tables US.4c, DE.4c, etc.

III- The changing nature of wealth 1700-2010

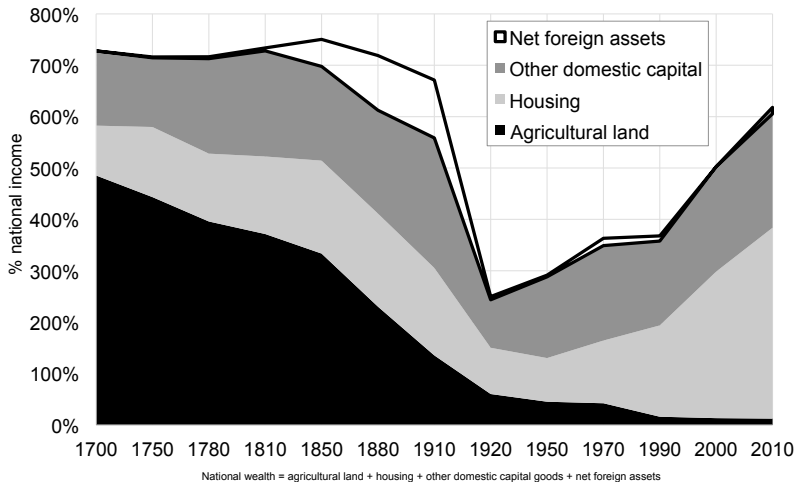
What do we know about pre-1870 β ?

- ▶ In Europe $\beta \approx 600\%-700\%$ throughout 18c-19c
- ▶ Not far from today despite considerable changes in nature of wealth
- ▶ How to explain pre-1870 β levels?
 - ▶ One possible explanation is $\beta = s/g$
 - ▶ But relative price effects also possible (land values)
 - ▶ s series too uncertain to decompose β dynamics
 - ▶ “Pure” land values could be less than 50% Y or up to 200%

In order to make progress on these questions, useful to compare value of land in Old Europe and in New World

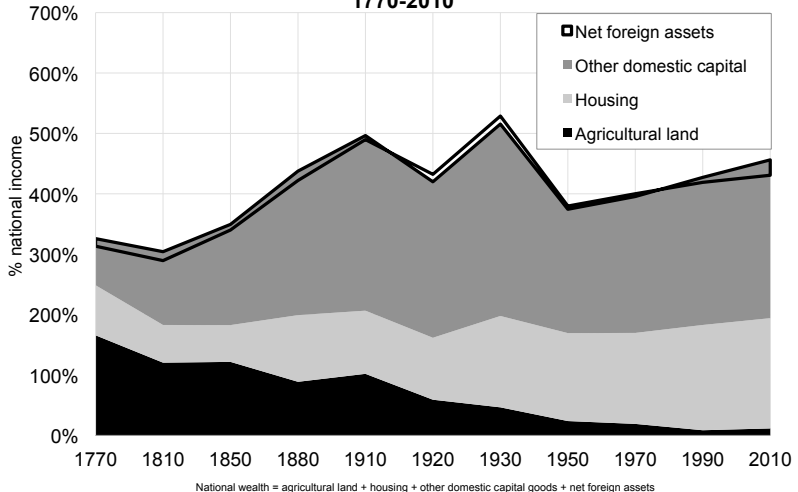
In 18c Old World, land/ Y as high as 400%

**Figure 9: The changing nature of national wealth: France
1700-2010**

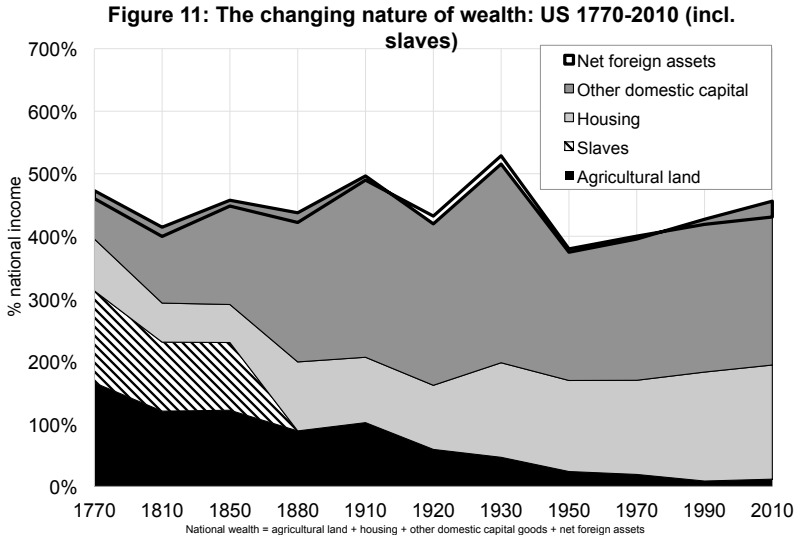


Land in late 18c US was much less than in Old World: abundance effect with $\sigma < 1$

**Figure 10: The changing nature of national wealth: US
1770-2010**

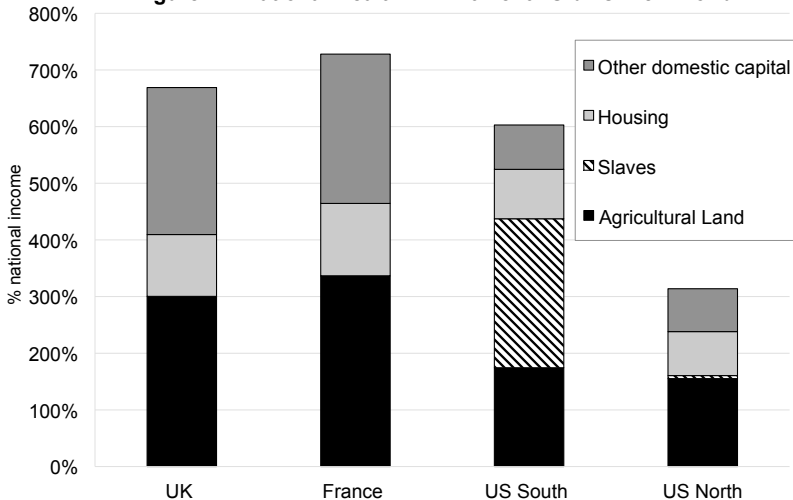


Lower land values in the US were to some extent compensated by the slavery system



There are two ways to be rich in 1810

Figure 12: National wealth in 1770-1810: Old vs. New world



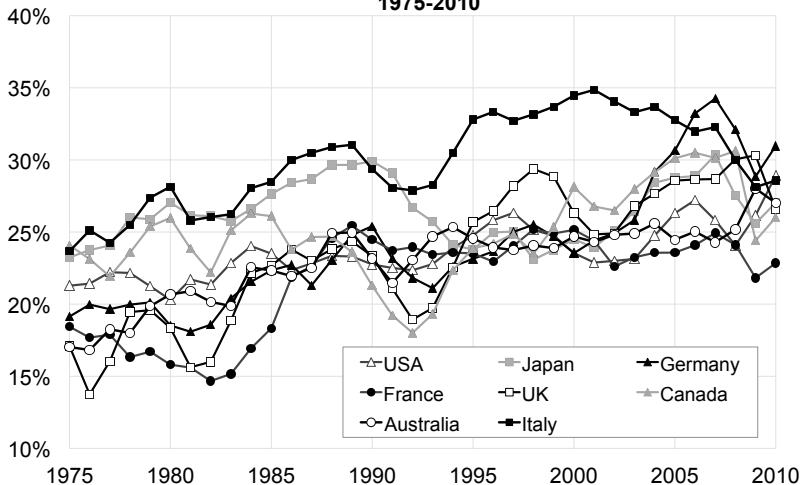
IV - Implications of the return of high wealth-income ratios

The return of high β is not bad per se but raises new issues

- ▶ Wealth inequality likely to matter more than in postwar period
- ▶ Implications for optimal taxation
- ▶ Wide variations in $\beta = s/g$ imply potentially very large net foreign asset positions...
- ▶ ... or domestic asset price bubbles (Spain, Japan)
- ▶ Rising capital shares with K-L elasticity $\sigma > 1$

With $\sigma > 1$, the rise of β can explain the rise of capital share $\alpha = r\beta$

Figure 13: Capital shares in factor-price national income
1975-2010



σ does not have to be hugely > 1 to account for observed trends

CES production: $F(K, L) = [aK^{\frac{\sigma-1}{\sigma}} + (1-a)L^{\frac{\sigma-1}{\sigma}}]^{\frac{\sigma}{\sigma-1}}$

$r = F_K = a\beta_K^{-1/\sigma}$ and capital share $\alpha = r\beta_K = a\beta_K^{\frac{\sigma-1}{\sigma}}$

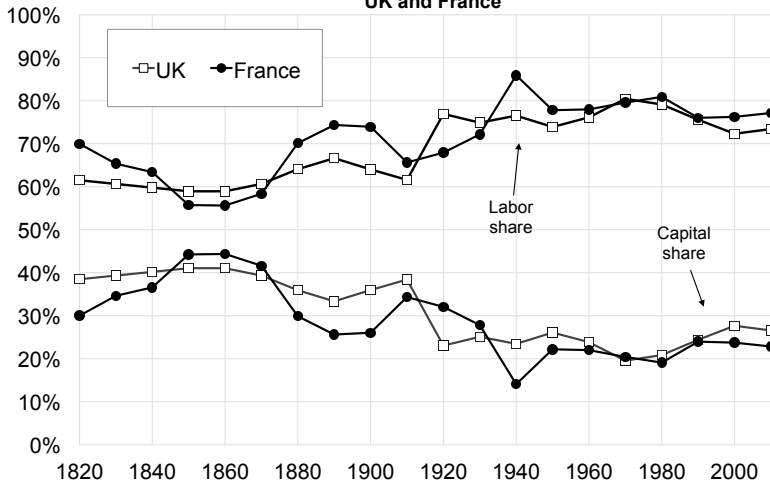
- ▶ If $\sigma = 1.5$, capital share rises from $\alpha = 28\%$ to $\alpha = 36\%$ when β_K rises from 250% to 500%
- ▶ In case β_K reaches 800%, α would reach 42%
- ▶ In case $\sigma = 1.8$, α would be as large as 53%



There are powerful forces in the one-good model that push toward high α

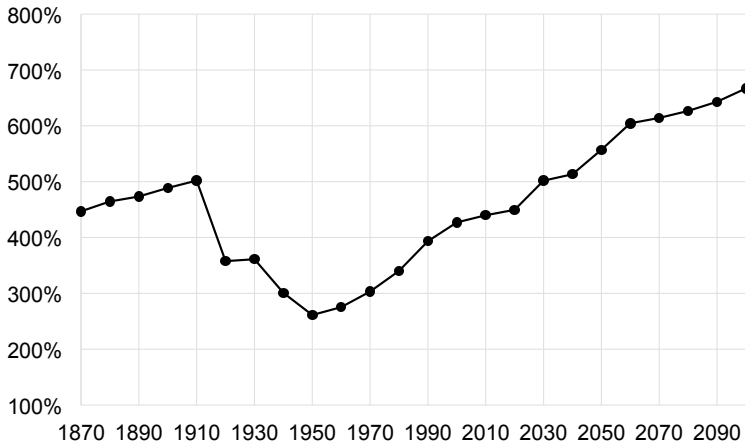
Will α get back to its 19c level?

Figure 15: Factor shares in factor-price national income 1820-2010:
UK and France



With g low and $\sigma > 1$ the rise of human capital may turn out to be an illusion

**Figure 16: World private wealth / national income ratio
1870-2100**



Authors' computations and simulations using country national accounts and UN growth projections. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors)

Conclusion: capital is back

- ▶ Low β in 1950s-70s Europe were an anomaly
- ▶ With low growth, long run β can be very large (600%-700% or more). Key is $\beta = s/g$
- ▶ The return of high β raises a new set of issues about capital regulation and taxation
- ▶ Next steps:
 - ▶ **Plug distributions:** Will China or global billionaires own the world? With low g both divergence can occur
 - ▶ **Normative implications:** relative importance of inherited vs. self-made wealth: 1910-2010 U-shaped pattern in France; on-going work on UK, Germany, and US

Supplementary Slides

Figure 14: Average return on private wealth 1975-2010

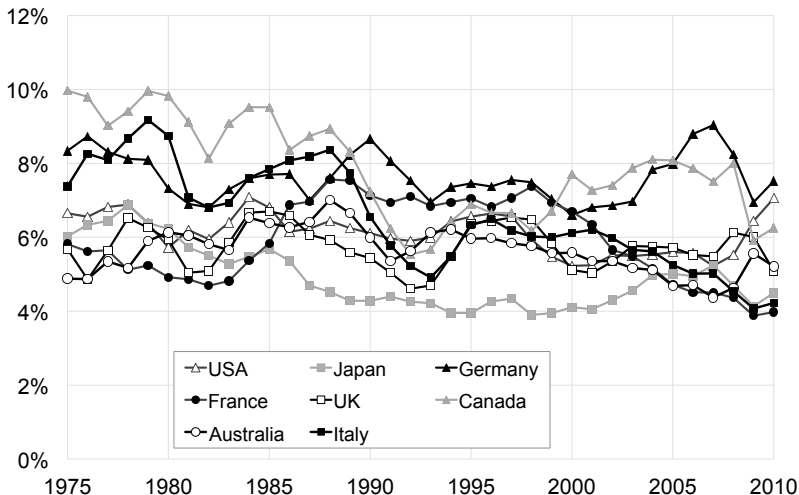


Table 3: Saving rates 1970-2010: national vs. private

<i>Average saving rates 1970-2010 (% national income)</i>	Net national saving (private + government)	Net private savings (personal + corporate)	<i>incl. personal savings</i>	<i>incl. corporate savings (retained earnings)</i>	Net government saving
U.S.	5.2%	7.7%	4.6% 60%	3.1% 40%	-2.4%
Japan	14.6%	14.6%	6.8% 47%	7.8% 53%	0.0%
Germany	10.2%	12.2%	9.4% 76%	2.9% 24%	-2.1%
France	9.2%	11.1%	9.0% 81%	2.1% 19%	-1.9%
U.K.	5.3%	7.3%	2.8% 38%	4.6% 62%	-2.0%
Italy	8.5%	15.0%	14.6% 97%	0.4% 3%	-6.5%
Canada	10.1%	12.1%	7.2% 60%	4.9% 40%	-2.0%
Australia	8.9%	9.9%	5.9% 60%	3.9% 40%	-0.9%

Authors' computations using country national accounts. 1970-2010 averages are obtained by weighting yearly saving rates by real national income.

Table 5: Accumulation of national wealth in rich countries, 1970-2010: domestic capital vs foreign wealth

	1970 national wealth / national income ratio		2010 national wealth / national income ratio		1970-2010 rise in national wealth / national income ratio	
	<i>incl. Domestic capital</i>	<i>incl. Foreign wealth</i>	<i>incl. Domestic capital</i>	<i>incl. Foreign wealth</i>	<i>incl. Domestic capital</i>	<i>incl. Foreign wealth</i>
U.S.	404%		431%		27%	
	399%	4%	456%	-25%	57%	-30%
Japan	359%		616%		256%	
	356%	3%	548%	67%	192%	64%
Germany	313%		416%		102%	
	305%	8%	377%	39%	71%	31%
France	351%		605%		254%	
	340%	11%	618%	-13%	278%	-24%
U.K.	365%		527%		163%	
	359%	6%	548%	-20%	189%	-26%
Italy	259%		609%		350%	
	247%	12%	640%	-31%	392%	-42%
Canada	284%		412%		128%	
	325%	-41%	422%	-10%	97%	31%
Australia	391%		584%		194%	
	410%	-20%	655%	-70%	244%	-50%

Table 7: Domestic capital accumulation in rich countries, 1970-2010: housing vs other domestic capital

	1970 domestic capital / national income ratio		2010 domestic capital / national income ratio		1970-2010 rise in domestic capital / national income ratio	
	<i>incl. Housing</i>	<i>incl. Other domestic capital</i>	<i>incl. Housing</i>	<i>incl. Other domestic capital</i>	<i>incl. Housing</i>	<i>incl. Other domestic capital</i>
U.S.	399% 142%	257%	456% 182%	274%	57% 41%	17%
Japan	356% 131%	225%	548% 220%	328%	192% 89%	103%
Germany	305% 129%	177%	377% 241%	136%	71% 112%	-41%
France	340% 104%	236%	618% 371%	247%	278% 267%	11%
U.K.	359% 98%	261%	548% 300%	248%	189% 202%	-13%
Italy	247% 107%	141%	640% 386%	254%	392% 279%	113%
Canada	325% 108%	217%	422% 208%	213%	97% 101%	-4%
Australia	410% 172%	239%	655% 364%	291%	244% 193%	52%

1910-1950: war destructions \approx a third of the fall of β in Germany and France

Table 10: Accumulation of national wealth in rich countries, 1910-1950

	National wealth-national income ratios		Decomposition of 1950 national wealth-national income ratio			
	β (1910)	β (1950)	Initial wealth effect	Cumulated new savings	Cumulated war destructions	Capital gains or losses
U.S.	469%	380%	132%	193%	0%	55%
Germany	637%	223%	400%	109% 31%	-120% 29%	-165% 40%
France	747%	261%	421%	144% 38%	-132% 27%	-172% 35%
U.K.	719%	208%	409%	75% 46%	-19% 4%	-256% 50%

Germany's national wealth-income ratio fell from 637% to 223% between 1910 and 1950. 31% of the fall can be attributed to insufficient saving, 29% to war destructions, and 40% to real capital losses.